Goodness of Fit Tests (Year 1) (From OCR 4768)

Q1, (Jun 2010, Q3b)

H₀: Stock market prices can be modelled by Benford's Law.

H₁: Stock market prices can not be modelled by Benford's Law.

Prob	0.301	0.176	0.125	0.097	0.079	0.067	0.058	0.051	0.046
Exp f	60.2	35.2	25.0	19.4	15.8	13.4	11.6	10.2	9.2
Obs f	55	34	27	16	15	17	12	15	9

$X^2 = 0.44917 + 0.04091 + 0.16 + 0.59588 + 0.04051$	Ĺ
$+\ 0.96716 + 0.01379 + 2.25882 + 0.00435$	
=4.5305(9)	

Refer to χ_8^2 .

Upper 5% point is 13.36. Not significant.

Suggests Benford's Law provides a reasonable model in the context of share prices.

 $\begin{array}{ll} M1 & Probs \times 200 \ for \ expected \ frequencies. \\ & All \ correct. \end{array}$

M1 Calculation of X^2 .

A1 c.a.o.

M1 Allow correct df (= cells – 1) from wrongly grouped table and ft. Otherwise, no ft if wrong. $P(X^2 > 4.53059) = 0.80636$.

A1 No ft from here if wrong.

A1 ft only c's test statistic.

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[7]

Q2, (Jan 2013, Q4b)

H ₀ : The random number function is performing as it should.	B1	Both hypotheses. Must be the right way round. Allow use of the uniform distribution/model. Do not accept "data fit model" oe.
H ₁ : The random number function is not performing as it should.		
All expected frequencies are 10	B1	
$X^2 = 1.6 + 0.4 + 0.1 + 1.6 + 0.4 + 0.1 + 2.5 + 2.5 + 1.6 + 1.6$	M1	Calculation of X^2 .
= 12.4	A1	c.a.o.
Refer to χ_9^2 .	M1	Allow correct df (= cells – 1) from wrongly grouped table and ft. Otherwise, no ft if wrong. $P(X^2 > 12.4) = 0.1916$.
Upper 10% point is 14.68.	A1	No ft from here if wrong.
Not significant.	A1	ft only c's test statistic.
Insufficient evidence to suggest that the	A1	ft only c's test statistic. Conclusion in context.
random number function is not performing as it should.		Allow in terms of the uniform distribution/model. Do not accept "data fit model" oe.
	[8]	

Q3, (Jun 2016, Q2a)

H ₀ : The (genetic) model fits the data.	B1	Both hypotheses; Not 'data fits model'
H ₁ : The (genetic) model does not fit the data		
Observed 125 37 32 6		
Expected 112.5 37.5 12.5	B1	Expected values correct
0.000 0.0007 0.0007 0.00	3.41	(O E)2 /E (-1111111111111111111
Cont's 1.3889 0.0067 0.8067 3.38	M1	use of (0-E) ² /E (at least one correct)
	A1	all correct to 3dp where appropriate
$X^2 = 5.582$	A1	cao (3sf or 4sf)
Degrees of freedom = 3	B1	no FT if wrong (can be implied by 9.348)
Critical value = 9.348	B1	no FT if wrong
$5.582 < 9.348 \rightarrow \text{cannot reject H}_0$	M1	FT their X ²
The data give no reason to doubt the genetic model	E1	Do not accept data fits model;
The data give no reason to doubt the genetic model		but 'Evidence suggests that model first the data' is fine
	[9]	Late Evidence edggeste that model mot the data is into

Q4, (Jun 2017, Q2ii)

H ₀ : Judges awarded the same number of each mark	
H ₁ : Judges did not award the same number of each	
mark.	

observed	5	6	10	9	14	16	14	6
expected	10	10	10	10	10	10	10	10

$$\chi^2 = 2.5 + 1.6 + 0 + 0.1 + 1.6 + 3.6 + 1.6 + 1.6$$

$$= 12.6$$
Refer to χ^2

Refer to χ_7^2

The 10% critical value is 12.02.

12.6 > 12.02 so significant

There is sufficient evidence that judges have not been awarding the same number of each mark.

B1	Both hypotheses. Must be in correct context. Allow
	'uniform distribution' or 'in equal proportions'.
	'Model fits data' or 'belief is justified' is ok.
	Do not accept 'data fits model' oe'.

B1 For expected frequencies.

Calculation of χ^2 . (if 12.6 not seen, must see evidence M1 of calculation)

A1 cao.

[8]

M1 No ft if wrong. **A1** No ft if wrong.

M1 ft their test statistic

Must be in context and mention 'evidence'. ('organiser's belief' is sufficient context)

Q5, (OCR 4734, Jun 2014, Q2)

H ₀ : The data can be modelled by the theory	B1	For both	Allow compatible.
H ₁ : The data can't be modelled by the theory.			
Expected values 918, 306, 306, 102	B1	Can be implied by 7.43	
$TS = \frac{(865 - 918)^2}{918} + \dots$	M1		
= 7.43	A1		
$TS < 7.815$, do not reject H_0	M1	ft TS	p>0.05 do not reject H ₀
There is insufficient evidence to conclude that the data can't be modelled by the theory	A1	ft TS	p=0.05939 and conclusion
	[6]		

A1

Q6, (OCR 4734, Jun 2012, Q7i)

$H_0: p_1 = p_2 = p_3 = 1/3$, $H_1:$ Not all equal oe eg in words	B1	$p=\frac{1}{3}$ only insufficient.	
E-values all 30	B1		
$\chi^2 = (1^2 + 5^2 + 4^2)/30$	M1		
= 1.4	A1	Accept 1.39,1.399 etc	
(Critical value = 5.991)			
Compare χ^2 with CV and do not reject H ₀ . Insufficient evidence	M1	With valid comparison	
that groups not randomly chosen.oe	A1ft	or Accept that groups randomly chosen.	
	[6]		